



Procesiranje signala

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"This project has been funded with support from the European Commission. This publication [communication] reflects the views only of the author, and the Commission cannot be held responsible for any use which may be made of the information contained therein"

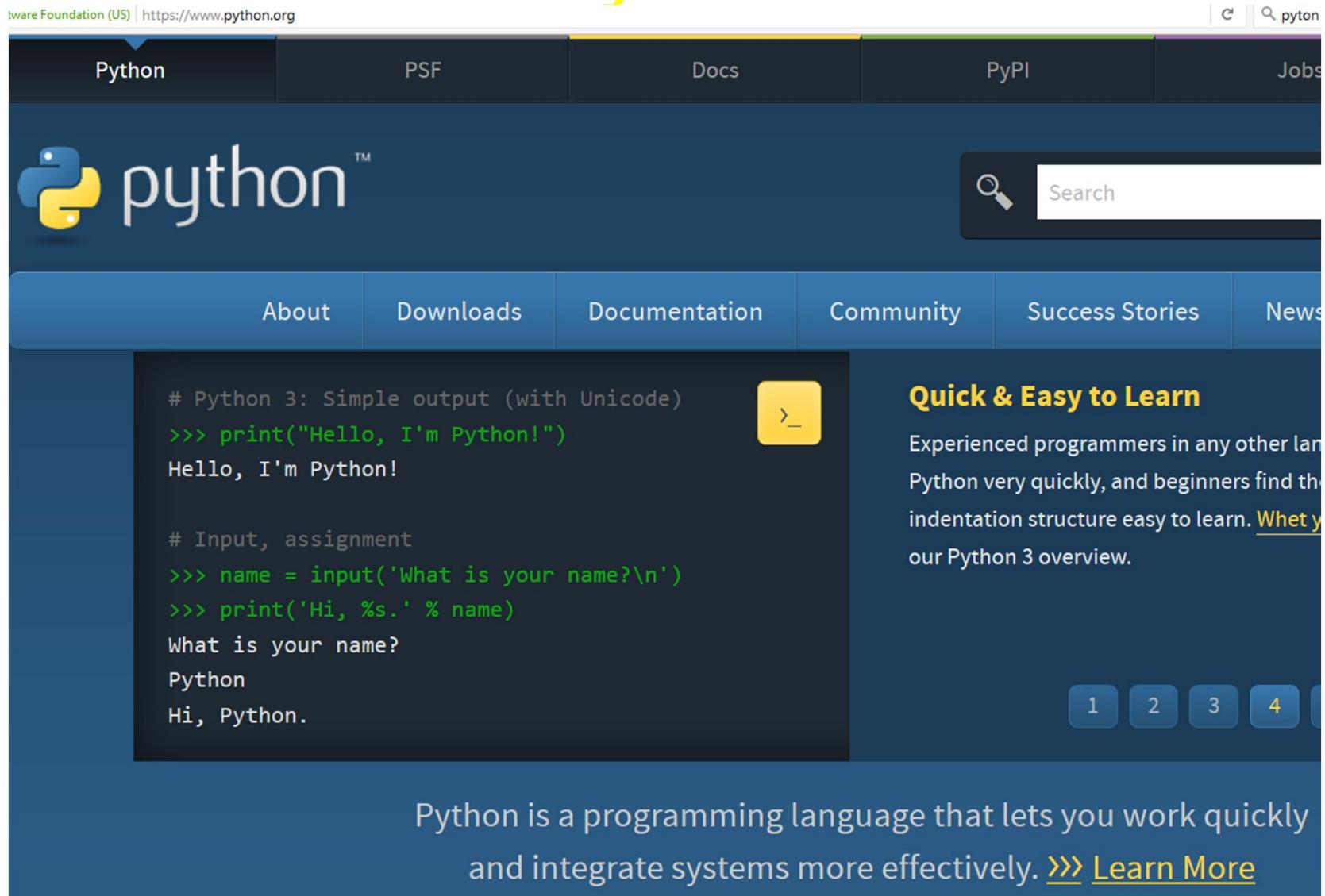
Sadržaj predmeta, Teorijska nastava

1. Uvodno predavanje. Upoznavanje sa planom i programom, ciljevima, ishodom i metodama.
2. Šta je procesiranje signala, istorijski pregled obrade signala, primeri primene.
3. Vizuelizacija signala (Python, Excel).
4. Kompleksni ekponencijalni diskretni signali. Primer sinteze muzičkog signala.
5. Furijeova analiza: Diskretna Furijeova transformacija (DFT) i serija (DFS). Brza Furijeova transformacija (Fast Fourier transform, FFT) i primena za spektralne analizatore i osciloskope.
6. Linearani filtri: konvolucija, idealni i realni filtri, dizajn filtra. Primena konvolucije u GPS sistemima.

...

Python

Software Foundation (US) | <https://www.python.org> |   python



The screenshot shows the Python.org homepage. At the top, there's a navigation bar with links for Python, PSF, Docs, PyPI, and Jobs. Below the header is a large Python logo. To the right is a search bar with a magnifying glass icon and the word "Search". The main content area features two code snippets in a terminal-like interface. The first snippet shows a simple print statement: "# Python 3: Simple output (with Unicode)\n>>> print(\"Hello, I'm Python!\")\nHello, I'm Python!". The second snippet shows input and output: "# Input, assignment\n>>> name = input('What is your name?\n')\n>>> print('Hi, %s.' % name)\nWhat is your name?\nPython\nHi, Python.". To the right of these snippets is a yellow button with a right-pointing arrow. To the right of the button is a section titled "Quick & Easy to Learn" with the subtext: "Experienced programmers in any other language can learn Python very quickly, and beginners find the indentation structure easy to learn. [What you need to know](#) is our Python 3 overview." At the bottom, there are navigation links numbered 1 through 4.

Python 3: Simple output (with Unicode)

```
>>> print("Hello, I'm Python!")
```

Hello, I'm Python!

Input, assignment

```
>>> name = input('What is your name?\n')
```

```
>>> print('Hi, %s.' % name)
```

What is your name?

Python

Hi, Python.

Quick & Easy to Learn

Experienced programmers in any other language can learn Python very quickly, and beginners find the indentation structure easy to learn. [What you need to know](#) is our Python 3 overview.

1 2 3 4

Python is a programming language that lets you work quickly and integrate systems more effectively. [»» Learn More](#)

Python

- Easy to learn,
- powerful programming language
- Efficient high-level data structures
- Simple and effective object-oriented
- Dynamic typing, interpreted
- Scripting
- Rapid application development
- On most platforms

Python

- Freely available in source or binary form
- Freely distributed
- Modules programs, tools, documentation
 - search-and-replace over a large number of text files, or rename and rearrange photo files in a complicated way
 - small custom database,
 - specialized GUI application,
 - simple game

Why Python?

- Write/compile/test/re-compile cycle too slow
- Offers much more error checking
- Very-high-level language
- Split program into modules that can be reused in other programs
- Interpreted language
- Save considerable time during program development because no compilation and linking is necessary

Why Python?

- Interpreter used interactively
- Write throw-away programs
- Test functions during bottom-up program development
- Handy desk calculator
- Express complex operations in a single statement
- no variable or argument declarations are necessary

Python

Interactive Help in Python Shell

<code>help()</code>	Invoke interactive help
<code>help(<i>m</i>)</code>	Display help for module <i>m</i>
<code>help(<i>f</i>)</code>	Display help for function <i>f</i>
<code>dir(<i>m</i>)</code>	Display names in module <i>m</i>

Small Operator Precedence Table

<code>func_name(args, ...)</code>	Function call
<code>x[index : index]</code>	Slicing
<code>x[index]</code>	Indexing
<code>x.attribute</code>	Attribute reference
<code>**</code>	Exponentiation
<code>*, /, %</code>	Multiply, divide, mod
<code>+, -</code>	Add, subtract
<code>>, <, <=, >=, !=, ==</code>	Comparison
<code>in, not in</code>	Membership tests
<code>not, and, or</code>	Boolean operators NOT, AND, OR

Python

Module Import

```
import module_name  
from module_name import name , ...  
from module_name import *
```

Common Data Types

Type	Description	Literal Ex
int	32-bit Integer	3, -4
long	Integer > 32 bits	101L
float	Floating point number	3.0, -6.55
complex	Complex number	1.2J
bool	Boolean	True, False
str	Character sequence	“Python”
tuple	Immutable sequence	(2, 4, 7)
list	Mutable sequence	[2, x, 3.1]
dict	Mapping	{ x:2, y:5 }

Python

Common Syntax Structures

Assignment Statement

var = *exp*

Console Input/Output

var = input([*prompt*])

var = raw_input([*prompt*])

print *exp*[*i*], ...

Selection

if (*boolean_exp*):
 stmt ...

[elif (*boolean_exp*):
 stmt ...] ...

[else:

stmt ...]

Repetition

while (*boolean_exp*):
 stmt ...

Traversal

for *var* in *traversable_object*:
 stmt ...

Python

Function Definition

```
def function_name( parameters ):  
    stmt ...
```

Function Call

```
function_name( arguments )
```

Class Definition

```
class Class_name [ (super_class) ]:  
    [ class variables ]  
    def method_name( self, parameters ):  
        stmt
```

Object Instantiation

```
obj_ref = Class_name( arguments )
```

Method Invocation

```
obj_ref.method_name( arguments )
```

Exception Handling

```
try:  
    stmt ...  
except [exception_type] [, var]:  
    stmt ...
```

Python

Common Built-in Functions

Function	Returns
<code>abs(x)</code>	Absolute value of <i>x</i>
<code>dict()</code>	Empty dictionary, eg: <code>d = dict()</code>
<code>float(x)</code>	int or string <i>x</i> as float
<code>id(obj)</code>	memory addr of <i>obj</i>
<code>int (x)</code>	float or string <i>x</i> as int
<code>len(s)</code>	Number of items in sequence <i>s</i>
<code>list()</code>	Empty list, eg: <code>m = list()</code>
<code>max(s)</code>	Maximum value of items in <i>s</i>
<code>min(s)</code>	Minimum value of items in <i>s</i>
<code>open(f)</code>	Open filename <i>f</i> for input
<code>ord(c)</code>	ASCII code of <i>c</i>
<code>pow(x,y)</code>	<i>x</i> ** <i>y</i>
<code>range(x)</code>	A list of <i>x</i> ints 0 to <i>x</i> - 1
<code>round(x,n)</code>	float <i>x</i> rounded to <i>n</i> places
<code>str(obj)</code>	str representation of <i>obj</i>
<code>sum(s)</code>	Sum of numeric sequence <i>s</i>
<code>tuple(items)</code>	tuple of <i>items</i>
<code>type(obj)</code>	Data type of <i>obj</i>

Python

Common Math Module Functions

Function	Returns (all float)
<code>ceil(x)</code>	Smallest whole nbr $\geq x$
<code>cos(x)</code>	Cosine of x radians
<code>degrees(x)</code>	x radians in degrees
<code>radians(x)</code>	x degrees in radians
<code>exp(x)</code>	e^{**x}
<code>floor(x)</code>	Largest whole nbr $\leq x$
<code>hypot(x, y)</code>	$\sqrt{x^2 + y^2}$
<code>log(x [, base])</code>	Log of x to $base$ or natural log if $base$ not given
<code>pow(x, y)</code>	x^{**y}
<code>sin(x)</code>	Sine of x radians
<code>sqrt(x)</code>	Positive square root of x
<code>tan(x)</code>	Tangent of x radians
<code>pi</code>	Math constant pi to 15 sig figs
<code>e</code>	Math constant e to 15 sig figs

Python

Common String Methods

S.method()	Returns (str unless noted)
capitalize	S with first char uppercase
center(<i>w</i>)	S centered in str <i>w</i> chars wide
count(<i>sub</i>)	int nbr of non-overlapping occurrences of <i>sub</i> in S
find(<i>sub</i>)	int index of first occurrence of <i>sub</i> in S or -1 if not found
isdigit()	bool True if S is all digit chars, False otherwise
islower()	bool True if S is all lower/upper case chars, False otherwise
join(<i>seq</i>)	All items in <i>seq</i> concatenated into a str, delimited by S
lower() upper()	Lower/upper case copy of S
lstrip() rstrip()	Copy of S with leading/ trailing whitespace removed, or both
split([<i>sep</i>])	List of tokens in S, delimited by <i>sep</i> ; if <i>sep</i> not given, delimiter is any whitespace

Python

Formatting Numbers as Strings

Syntax: “*format_spec*” % *numeric_exp*

***format_spec* syntax:** % *width.precision type*

- *width* (optional): align in number of columns specified; negative to left-align, precede with 0 to zero-fill
- *precision* (optional): show specified digits of precision for floats; 6 is default
- *type* (required): d (decimal int), f (float), s (string), e (float – exponential notation)
- Examples for x = 123, y = 456.789
 - “%6d” % x -> ... 123
 - “%06d” % x -> 000123
 - “%8.2f” % y -> .. 456.79
 - “8.2e” % y -> 4.57e+02
 - “-8s” % “Hello” -> Hello ...

Python

Common List Methods

<i>L.method()</i>	Result>Returns
<code>append(<i>obj</i>)</code>	Append <i>obj</i> to end of <i>L</i>
<code>count(<i>obj</i>)</code>	Returns int nbr of occurrences of <i>obj</i> in <i>L</i>
<code>index(<i>obj</i>)</code>	Returns index of first occurrence of <i>obj</i> in <i>L</i> ; raises ValueError if <i>obj</i> not in <i>L</i>
<code>pop([<i>index</i>])</code>	Returns item at specified <i>index</i> or item at end of <i>L</i> if <i>index</i> not given; raises IndexError if <i>L</i> is empty or <i>index</i> is out of range
<code>remove(<i>obj</i>)</code>	Removes first occurrence of <i>obj</i> from <i>L</i> ; raises ValueError if <i>obj</i> is not in <i>L</i>
<code>reverse()</code>	Reverses <i>L</i> in place
<code>sort()</code>	Sorts <i>L</i> in place

Python

Common Tuple Methods

T.method()	Returns
count(<i>obj</i>)	Returns nbr of occurrences of <i>obj</i> in <i>T</i>
index(<i>obj</i>)	Returns index of first occurrence of <i>obj</i> in <i>T</i> ; raises ValueError if <i>obj</i> is not in <i>T</i>

Common Dictionary Methods

D.method()	Result>Returns
clear()	Remove all items from <i>D</i>
get(<i>k</i> [, <i>val</i>])	Return <i>D[k]</i> if <i>k</i> in <i>D</i> , else <i>val</i>
has_key(<i>k</i>)	Return True if <i>k</i> in <i>D</i> , else False
items()	Return list of key-value pairs in <i>D</i> ; each list item is 2-item tuple
keys()	Return list of <i>D</i> 's keys
pop(<i>k</i> , [<i>val</i>])	Remove key <i>k</i> , return mapped value or <i>val</i> if <i>k</i> not in <i>D</i>
values()	Return list of <i>D</i> 's values

Python

Common File Methods

<i>F.method()</i>	Result>Returns
<code>read([n])</code>	Return str of next <i>n</i> chars from <i>F</i> , or up to EOF if <i>n</i> not given
<code>readline([n])</code>	Return str up to next newline, or at most <i>n</i> chars if specified
<code>readlines()</code>	Return list of all lines in <i>F</i> , where each item is a line
<code>write(s)</code>	Write str <i>s</i> to <i>F</i>
<code>writelines(L)</code>	Write all str in seq <i>L</i> to <i>F</i>
<code>close()</code>	Closes the file

Other Syntax

Hold window for user keystroke to close:

```
raw_input("Press <Enter> to quit.")
```

Prevent execution on import:

```
if __name__ == "__main__":
    main()
```

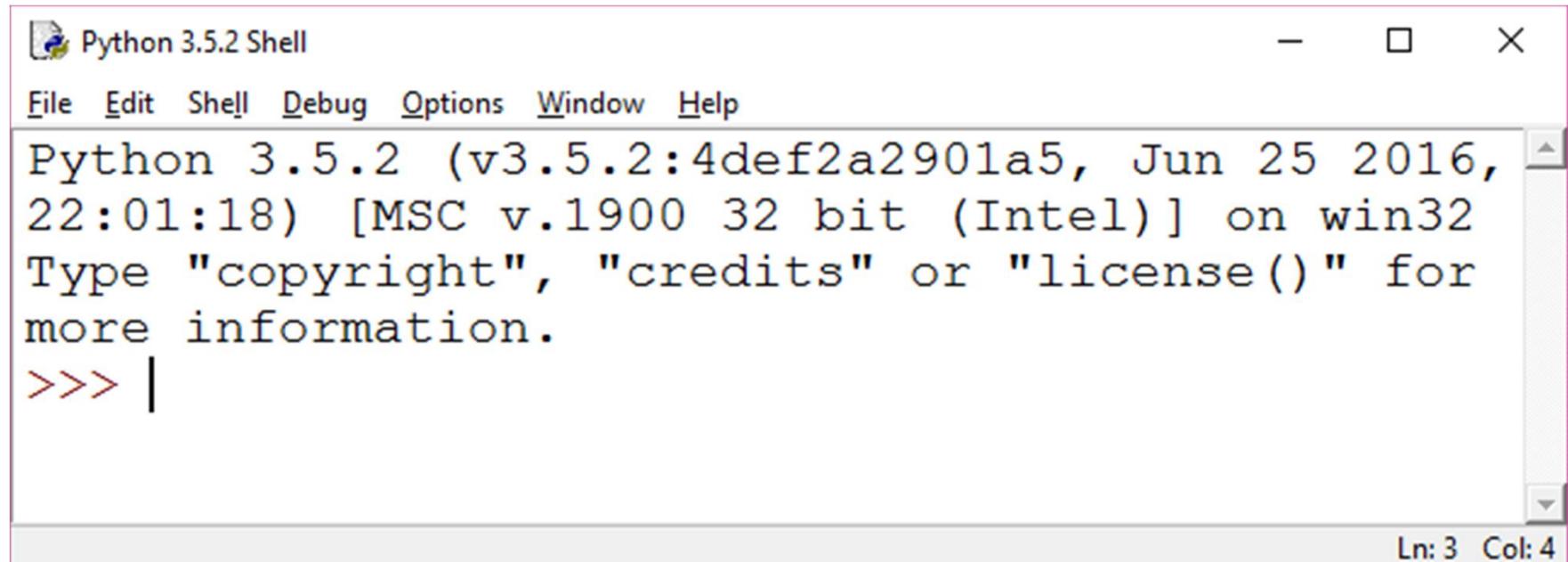
Python

Displayable ASCII Characters

32	SP	48	0	64	@	80	P	96	`	112	p
33	!	49	1	65	A	81	Q	97	a	113	q
34	"	50	2	66	B	82	R	98	b	114	r
35	#	51	3	67	C	83	S	99	c	115	s
36	\$	52	4	68	D	84	T	100	d	116	t
37	%	53	5	69	E	85	U	101	e	117	u
38	&	54	6	70	F	86	V	102	f	118	v
39	'	55	7	71	G	87	W	103	g	119	w
40	(56	8	72	H	88	X	104	h	120	x
41)	57	9	73	I	89	Y	105	i	121	y
42	*	58	:	74	J	90	Z	105	j	122	z
43	+	59	;	75	K	91	[107	k	123	{
44	,	60	<	76	L	92	\	108	l	124	
45	-	61	=	77	M	93]	109	m	125	}
46	.	62	>	78	N	94	^	110	n	126	~
47	/	63	?	79	O	95	_	111	o	127	DEL

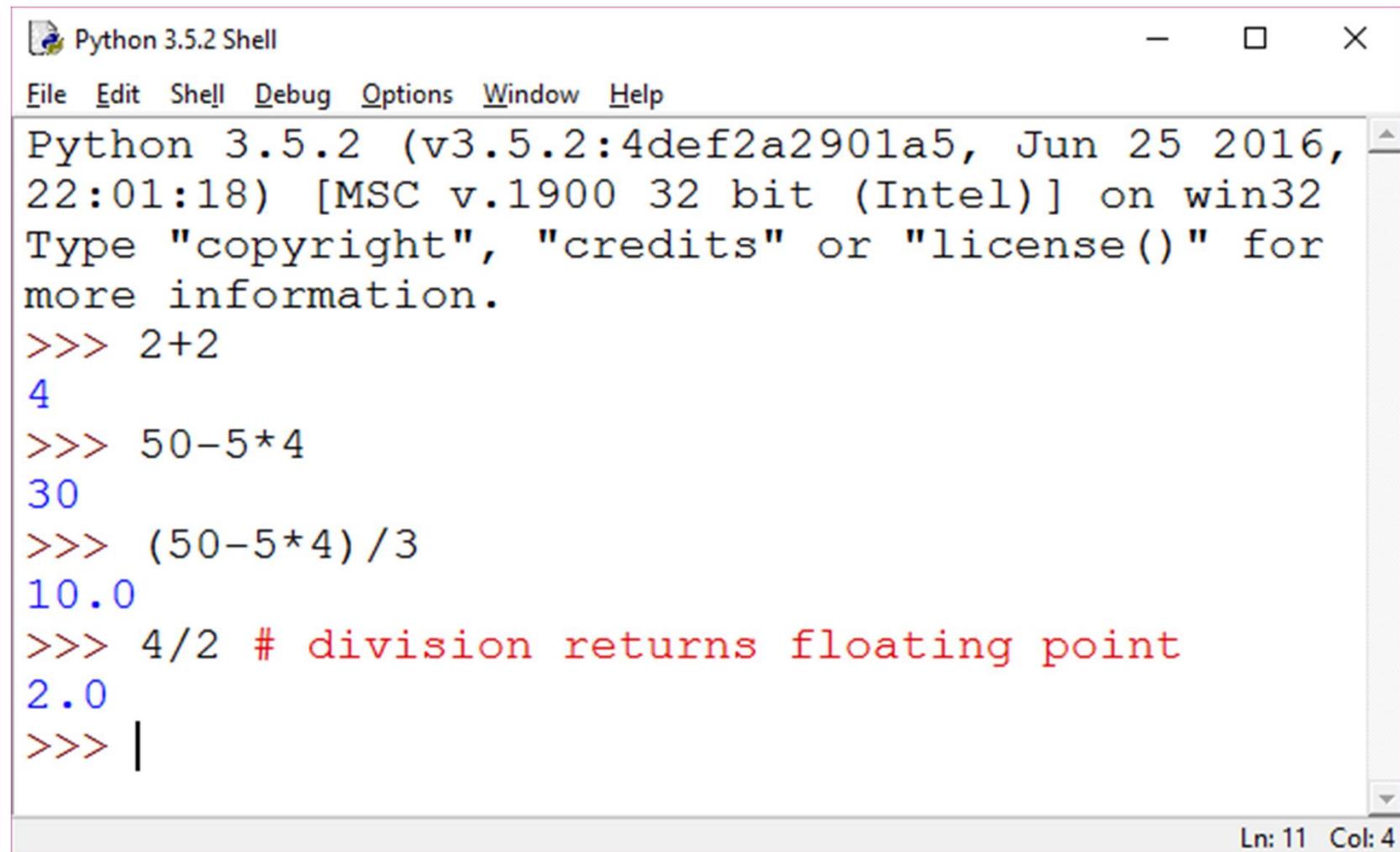
'\0' = 0, '\t' = 9, '\n' = 10

Python



The screenshot shows a window titled "Python 3.5.2 Shell". The menu bar includes File, Edit, Shell, Debug, Options, Window, and Help. The main area displays the Python welcome message: "Python 3.5.2 (v3.5.2:4def2a2901a5, Jun 25 2016, 22:01:18) [MSC v.1900 32 bit (Intel)] on win32 Type "copyright", "credits" or "license()" for more information." A command prompt ">>> |" is visible at the bottom left, and status indicators "Ln: 3 Col: 4" are at the bottom right.

Python



The screenshot shows the Python 3.5.2 Shell window. The title bar reads "Python 3.5.2 Shell". The menu bar includes File, Edit, Shell, Debug, Options, Window, and Help. The main window displays the Python interpreter's welcome message and several arithmetic operations:

```
Python 3.5.2 (v3.5.2:4def2a2901a5, Jun 25 2016,  
22:01:18) [MSC v.1900 32 bit (Intel)] on win32  
Type "copyright", "credits" or "license()" for  
more information.  
>>> 2+2  
4  
>>> 50-5*4  
30  
>>> (50-5*4)/3  
10.0  
>>> 4/2 # division returns floating point  
2.0  
>>> |
```

In the bottom right corner of the shell window, there is a status bar with "Ln: 11 Col: 4".

Python

The screenshot shows a Python 3.5.2 Shell window and a 'Kill?' dialog box.

Python 3.5.2 Shell Content:

```
Python 3.5.2 (v3.5.2:4def2a2901a5, Jun 25 2016, 22:01:18) [MSC v.1900 32 bit (Intel)] on win32
Type "copyright", "credits" or "license()" for more information.

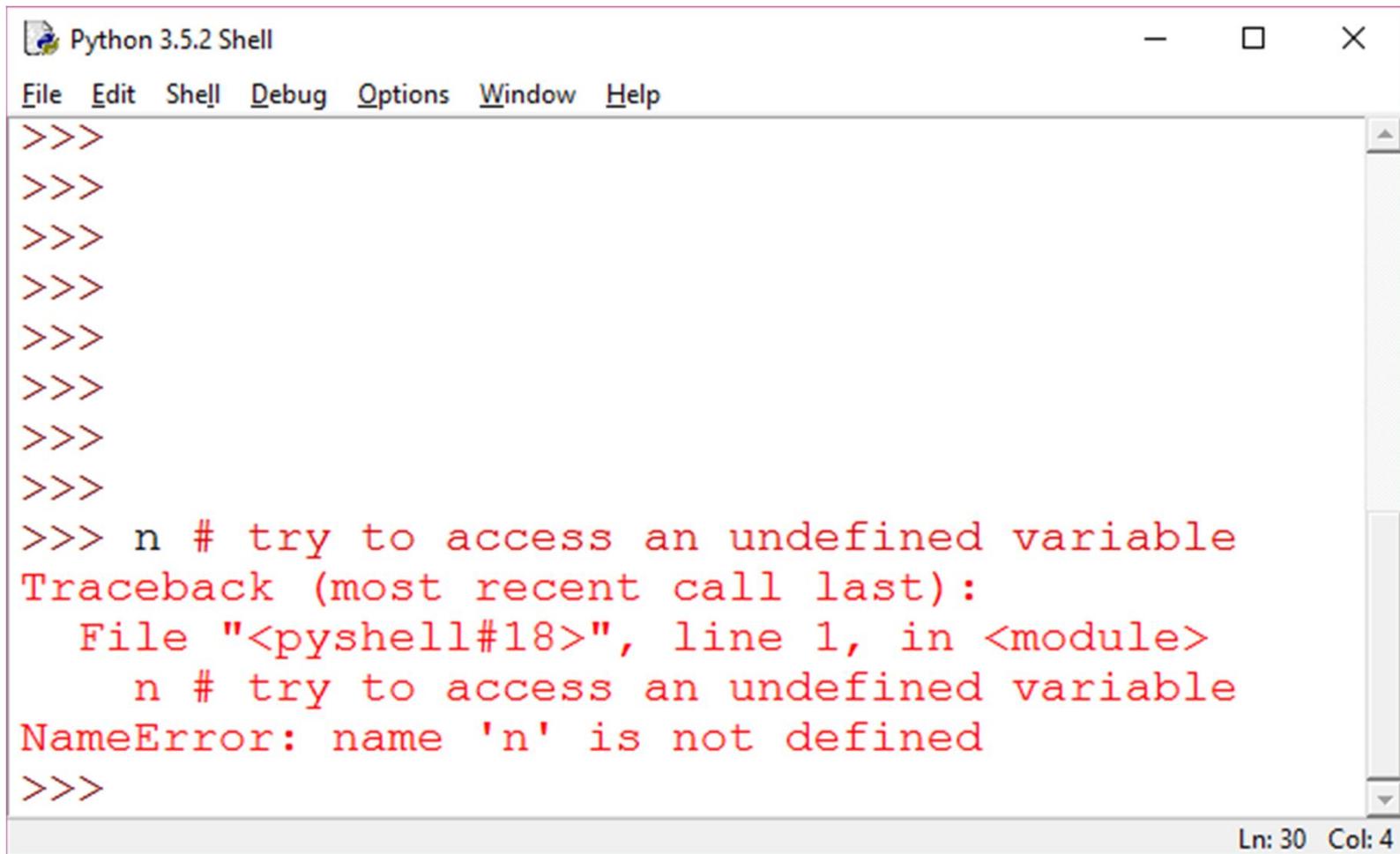
>>> 2+2
4
>>> 50-5*4
30
>>> (50-5*4)/3
10.0
>>> 4/2 # division returns float
2.0
>>> quit()
```

Kill? Dialog Box:

Your program is still running!
Do you want to kill it?

OK Cancel

Python



The screenshot shows a window titled "Python 3.5.2 Shell". The menu bar includes File, Edit, Shell, Debug, Options, Window, and Help. The main area displays a Python interactive session. The user has entered several blank lines starting with '>>>'. On the ninth line, they attempt to access an undefined variable 'n' with the command 'n # try to access an undefined variable'. This results in a Traceback error, which includes the file name '<pyshell#18>', line 1, in <module>, and the message 'n # try to access an undefined variable'. A NameError is then raised, stating 'NameError: name 'n' is not defined'. The session ends with another blank line starting with '>>>'. In the bottom right corner of the window, there is a status bar with 'Ln: 30 Col: 4'.

```
>>>
>>>
>>>
>>>
>>>
>>>
>>>
>>>
>>> n # try to access an undefined variable
Traceback (most recent call last):
  File "<pyshell#18>", line 1, in <module>
    n # try to access an undefined variable
NameError: name 'n' is not defined
>>>
```

the last printed expression is assigned to the variable `_`

```
>>> 18 / 100  
  
0.18  
  
>>> _  
  
0.18  
  
>>> total = 100 + _  
  
>>> total  
  
100.18  
  
>>>
```

```
>>> tax = 18 / 100  
  
>>>_  
  
Traceback (most recent call last):  
  
  File "<pyshell#2>", line 1, in <module>  
  
    -  
  
      NameError: name '_' is not defined
```

Strings

```
>>> 'ja sam Marko' # single quotes  
'ja sam Marko'
```

```
>>> 'doesn\'t' # use \' to escape the single quote...  
"doesn't"  
  
>>> "doesn't" # ...or use double quotes instead  
"doesn't"  
  
>>> '"Yes," he said.'  
'"Yes," he said.'  
  
>>> "\"Yes,\" he said."  
'"Yes," he said.'  
  
>>> '"Isn\'t," she said.'  
'"Isn\'t," she said.'
```

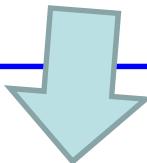
Strings - raw strings

```
>>> print('C:\some\name') # here \n means newline!
C:\some
ame

>>> print(r'C:\some\name') # note the r before the quote
C:\some\name
```

Strings - " " " " or ""

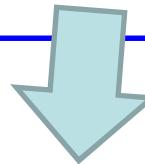
```
print("""\n\nUsage: thingy [OPTIONS]\n\n    -h            Display this usage message\n\n    -H hostname   Hostname to connect to\n\n""")
```



```
Usage: thingy [OPTIONS]\n\n    -h            Display this usage message\n\n    -H hostname   Hostname to connect to
```

concatenated with the + operator, and repeated with *

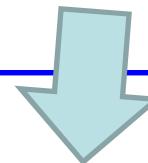
```
>>> # 3 times 'un', followed by 'ium'  
>>> 3 * 'un' + 'ium'
```



```
'unununium'
```

Lists

```
>>> squares = [1, 4, 9, 16, 25]  
>>> squares
```



```
[1, 4, 9, 16, 25]
```

```
>>> squares[-1]
```

```
25
```

```
>>> squares[0]
```

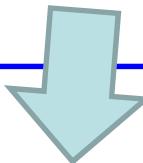
```
1
```

```
>>> squares[-3:]
```

```
[9, 16, 25]
```

Programming

```
>>> # Fibonacci series:  
... # the sum of two elements defines the next  
... a, b = 0, 1  
>>> while b < 10:  
... print(b)  
... a, b = b, a+b  
...
```

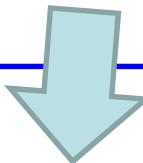


1
1
2
3
5
8

- ✓ multiple assignment
- ✓ while loop - condition ($b < 10$) remains true
- ✓ body of the loop is indented
- ✓ `print()` writes the value

Programming

```
>>> # Fibonacci series:  
... # the sum of two elements defines the next  
... a, b = 0, 1  
>>> while b < 10:  
... print(b)  
... a, b = b, a+b  
...
```



1
1
2
3
5
8

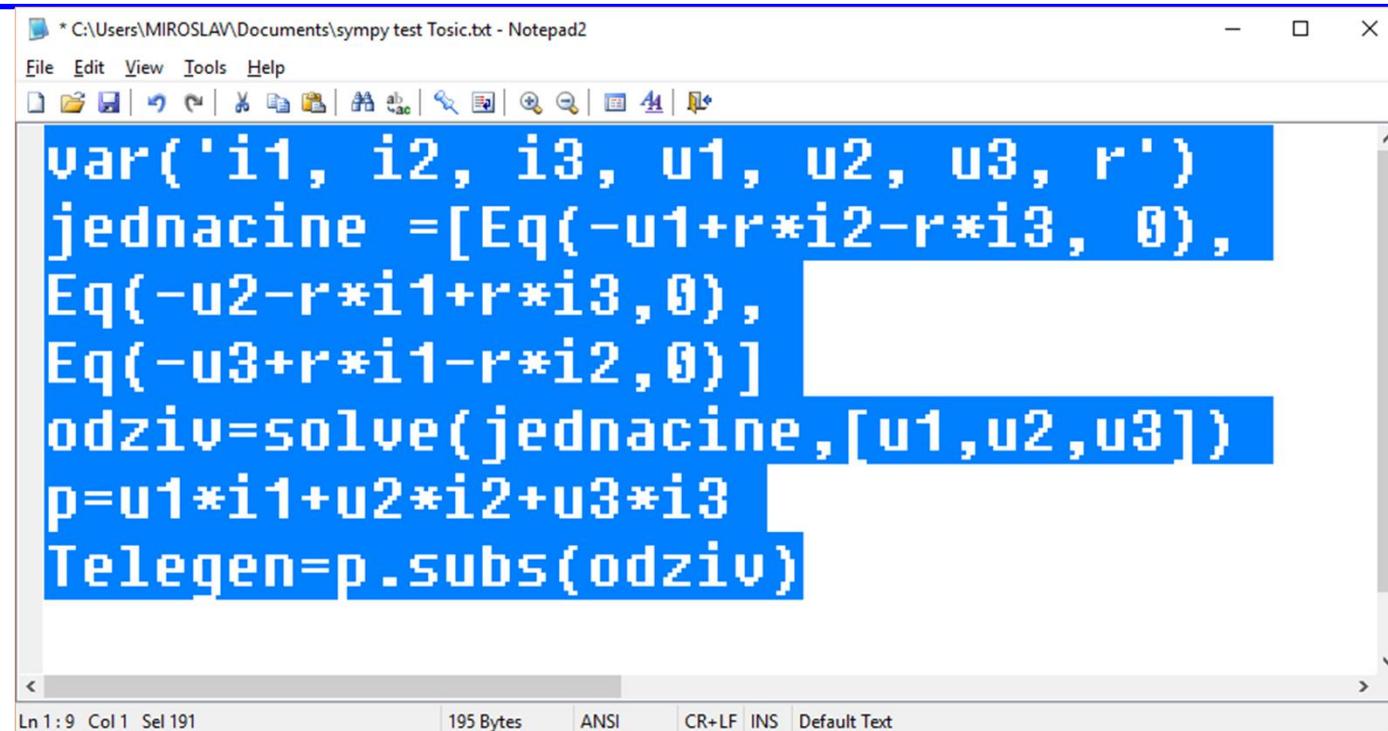
- ✓ multiple assignment
- ✓ while loop - condition ($b < 10$) remains true
- ✓ body of the loop is indented
- ✓ `print()` writes the value

Python console for SymPy 1.0 (Python 2.7.5)

These commands were executed:

```
>>> from __future__ import division
>>> from sympy import *
>>> x, y, z, t = symbols('x y z t')
>>> k, m, n = symbols('k m n', integer=True)
>>> f, g, h = symbols('f g h', cls=Function)
```

Documentation can be found at <http://docs.sympy.org/1.0>.



The screenshot shows a Notepad2 window with the following Python code:

```
var('i1, i2, i3, u1, u2, u3, r')
jednacine =[Eq(-u1+r*i2-r*i3, 0),
Eq(-u2-r*i1+r*i3, 0),
Eq(-u3+r*i1-r*i2, 0)]
odziv=solve(jednacine,[u1,u2,u3])
p=u1*i1+u2*i2+u3*i3
Telegen=p.subs(odziv)
```

The code defines variables `i1, i2, i3, u1, u2, u3, r`, sets up a list of three equations (`jednacine`), solves the system (`odziv`), calculates a sum (`p`), and substitutes the solution into `p` (`Telegen`).

These commands were executed:

```
>>> from __future__ import division
>>> from sympy import *
>>> x, y, z, t = symbols('x y z t')
>>> k, m, n = symbols('k m n', integer=True)
>>> f, g, h = symbols('f g h', cls=Function)
```

Documentation can be found at <http://docs.sympy.org/1.0>

```
>>> var('i1, i2, i3, u1, u2, u3, r')
... jednacine =[Eq(-u1+r*i2-r*i3, 0),
... Eq(-u2-r*i1+r*i3,0),
... Eq(-u3+r*i1-r*i2,0)]
... odziv=solve(jednacine,[u1,u2,u3])
... p=u1*i1+u2*i2+u3*i3
... Telegen=p.subs(odziv)
>>> Telegen
```

```
i1r (i2 - i3) + i2r (-i1 + i3) + i3r (i1 - i2)
```

```
>>>
```

▼ | < | > ▲

Evaluate **Clear** **Fullscreen**

```
* C:\Users\MIROSLAV\Documents\sympy test Totic.txt - Notepad2
File Edit View Tools Help
File Edit View Tools Help
var('i1, i2, i3, u1, u2, u3, r')
jednacine =[Eq(-u1+r*i2-r*i3, 0),
Eq(-u2-r*i1+r*i3,0),
Eq(-u3+r*i1-r*i2,0)]
odziv=solve(jednacine,[u1,u2,u3])
p=u1*i1+u2*i2+u3*i3
Telegen=p.subs(odziv)

Ln 1: 9 Col 1 Sel 191 195 Bytes ANSI CR+LF INS Default Text
```

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Ova prezentacija je nekomercijalna.

Slajdovi mogu da sadrže materijale preuzete sa Interneta, stručne i naučne građe, koji su zaštićeni Zakonom o autorskim i srodnim pravima.

Ova prezentacija se može koristiti samo privremeno tokom usmenog izlaganja nastavnika u cilju informisanja i upućivanja studenata na dalji stručni, istraživački i naučni rad i u druge svrhe se ne sme koristiti –

Član 44 - Dozvoljeno je bez dozvole autora i bez plaćanja autorske naknade za nekomercijalne svrhe nastave:
(1) javno izvođenje ili predstavljanje objavljenih dela u obliku neposrednog poučavanja na nastavi;
- ZAKON O AUTORSKOM I SRODΝIM PRAVIMA
("Sl. glasnik RS", br. 104/2009 i 99/2011)